$\qquad$

## Unit II

3. (a) Fit a second degree parabola to the following data :

| $\mathbf{X}$ | $\mathbf{Y}$ |
| :---: | :---: |
| 1989 | 352 |
| 1990 | 356 |
| 1991 | 357 |
| 1992 | 358 |
| 1993 | 360 |
| 1994 | 361 |
| 1995 | 361 |
| 1996 | 360 |
| 1997 | 359 |

(b) A manufacturer claims that only $4 \%$ of his products supplied by him are defective. A random sample of 600 products contained 36 defective. Test the claim of the manufacturer.7

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18B1
B.Tech. EXAMINATION, May 2019
(Second Semester)
(C-Scheme) (Main Only)
(CSE)
MATH102C
MATHEMATICS-II

Time : 3 Hours] [Maximum Marks : 75
Before answering the question-paper candidates should ensure that they have been supplied to correct and complete question-paper. No complaint, in this regard, will be entertained after the examination.

Note: Attempt Five questions in all, along with compulsory question, selecting one question from each Unit. All questions carry equal marks.
P.T.O.

## Unit I

1. (a) The distribution of marks in Hindi of 60 students of 10th class is as follows :

| Marks | Frequency |
| :---: | :---: |
| $0-10$ | 2 |
| $10-20$ | 3 |
| $20-30$ | 12 |
| $30-40$ | 8 |
| $40-50$ | 10 |
| $50-60$ | 17 |
| $60-70$ | 4 |
| $70-80$ | 3 |
| $80-90$ | 1 |

Calculate the measure of Kurtosis. 8
(b) Six dice are thrown 729 times. How many times do you expect at least three dice to show a five or six ?

7
2. (a) Six coins are tossed 6400 times. Using Poisson distribution determine the approximate probability of getting six heads $x$ times.8
(b) In a factory machines $\mathrm{A}, \mathrm{B}$ and C manufacture respectively $25 \%, 35 \%$ and $40 \%$ of the total bolt. There are $5 \%, 4 \%$ and $2 \%$ bolts are defective respectively. A bolt is drawn at random from the product and found defective. What is probability that it is drawn from machine B ?

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## (Compulsory Question)

9. (a) Write 3rd moment around mean and what it is called ?
(b) Write probability density function of the normal distribution and calculate total area under normal probability curve.
(c) Find the straight line that best fits the following data :

$$
\begin{array}{ccccccc}
x & : & 1 & 2 & 3 & 4 & 5 \\
y & : & 14 & 27 & 40 & 5 & 68
\end{array}
$$

(d) Discuss multinomial distribution in brief.
(e) The density function of a random varible X is given by :

$$
f(x)=k x(2-x)
$$

Find mean deviation about mean.
4. (a) A random sample of 900 members has a mean 3.4 cm . Can it be reasonably regarded as a sample from a large population of mean 3.2 cm and S.D. 2.3 cms .
(b) Describe Chi-square test for goodness of fit. The following table shows the distribution of digits in numbers choosen at random from a telephone directory.

| Digits | Frequency |
| :---: | :---: |
| 0 | 1026 |
| 1 | 1107 |
| 2 | 997 |
| 3 | 966 |
| 4 | 1075 |
| 5 | 933 |
| 6 | 1107 |
| 7 | 972 |
| 8 | 964 |
| 9 | 853 |

Test whether the digits may be taken to occur equally frequently in the directory.

## Unit III

5. (a) An urn contains 10 white and 3 black balls, while another urn contains 3 white and 4 black balls. Two balls are drawn from the first urn and put into the second urn and then a ball is drawn from the latter. What is the probability that it is white ball?
(b) A die is tossed thrice. A success is getting 1 or 6 on a toss. Find mean and variance of the number of successes.
6. (a) A box contains 5 red balls, 4 white balls and 3 blue balls. A ball is selected at random from the box, its colour is noted and then the ball is replaced. Find the probability that out of 6 balls selected in this manner, 3 are red, 2 are white and 1 is blue.

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(b) Find $\mathrm{E}(\mathrm{X}), \mathrm{E}\left(\mathrm{X}^{2}\right)$ and $\mathrm{E}[\mathrm{X}-\overline{\mathrm{X}}]^{2}$ for the probability distribution :

$$
\begin{array}{c:ccccc}
\mathrm{X} & : & 8 & 12 & 16 & 20 \\
\dot{\mathrm{P}}(\mathrm{x}) & : & \frac{1}{8} & \frac{1}{6} & \frac{3}{8} & \frac{1}{4} \\
\hline & \frac{1}{12}
\end{array}
$$

State Chebyshev's inequality.

## Unit IV

7. (a) A continuous random variable $X$ having values between 0 and 4 has a density function given by $\rho(\mathrm{X})=\frac{1}{2}-b X$, where $b$ is constant :
(i) Calculate $b$
(ii) Find $\mathrm{P}(1<\mathrm{X}<2)$.
(b) Discuss various properties of normal distribution function.

7
8. (a) Let the random variables $X$ and $Y$ have the joint pdf :

$$
f(x, y)=\left\{\begin{array}{lll}
x+y & 0<x<1, & 0<y<1 \\
0 & \text { elsewhere } &
\end{array}\right.
$$

Find covariance of X and Y . 7
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