

**18DD1908**

**M. Sc. EXAMINATION, 2020**

(Fourth Semester)

(C Scheme)

(Main Only)

MATHEMATICS

MAT618C

Operations Research

*Time : 3 Hours]*

*[Maximum Marks : 75*

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Before answering the question-paper candidates should ensure that they have been supplied to correct and complete question-paper. No complaint, in this regard, will be entertained after the examination.

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**Note :** Attempt *Five* questions in all, selecting *one* question from each Unit.  
Q. No. 9 is compulsory. All questions carry equal marks.

**Unit I**

1. Define LPP. Discuss unbounded and infinite solution in Graphical Method. Solve the LPP by Graphical Method : **15**

$$\text{Min. } Z = 20x_1 + 10x_2$$

Subject to

$$x_1 + 2x_2 \leq 40$$

$$3x_1 + x_2 \geq 30$$

$$4x_1 + 3x_2 \geq 60$$

and

$$x_1, x_2 \geq 0.$$

2. Use the simplex method to solve the following LPP : 15

$$\text{Max. } Z = 3x_1 + 5x_2 + 4x_3$$

Subject to

$$2x_1 + 3x_2 \leq 8$$

$$2x_1 + 5x_3 \leq 10$$

$$3x_1 + 2x_2 + 4x_3 \leq 15$$

and  $x_1, x_2, x_3 \geq 0.$

### Unit II

3. Given below is the unit cost array with supplies  $a_i$  ( $i = 1, 2, 3$ ) and demand  $b_j$  ( $j = 1, 2, 3, 4$ ) : 15

		Sink				
		1	2	3	4	$a_i$
Source	1	8	10	7	6	50
	2	12	9	4	7	40
	3	9	11	10	8	30
$b_j$		25	32	40	23	120

*Or*

Find the optimal solution to the above Hitchcock problem. 15

4. Solve the following minimal assignment problem : 15

		Job				
		1	2	3	4	5
Problem	A	8	4	2	6	1
	B	0	9	5	5	4
	C	3	8	9	2	6
	D	4	3	1	0	3
	E	9	5	8	9	5

### Unit III

5. Derive EOQ model for deterministic demand when replenishment rate is infinite and shortages are permitted. 15
6. Define Inventory. What are the advantages and disadvantages of having inventories ? 15

### Unit IV

7. Explain, how Gomory's cutting plane algorithm works. 15
8. Use the Kuhn-Tucker conditions to solve the following N.L.P. problem : 15

$$\text{Maximize } Z = 7x_1^2 - 6x_1 + 5x_2^2$$

Subject to

$$x_1 + 2x_2 \leq 10$$

$$x_1 - 3x_2 \leq 9$$

and  $x_1, x_2 \geq 0.$

9. (a) Define Dual Simplex method. 4
- (b) Define Hungarian method. 4
- (c) Explain the following : 4
- (i) Arrival pattern
- (ii) Service discipline.
- (d) Write the Kuhn-Tucker condition for NLPP. 3